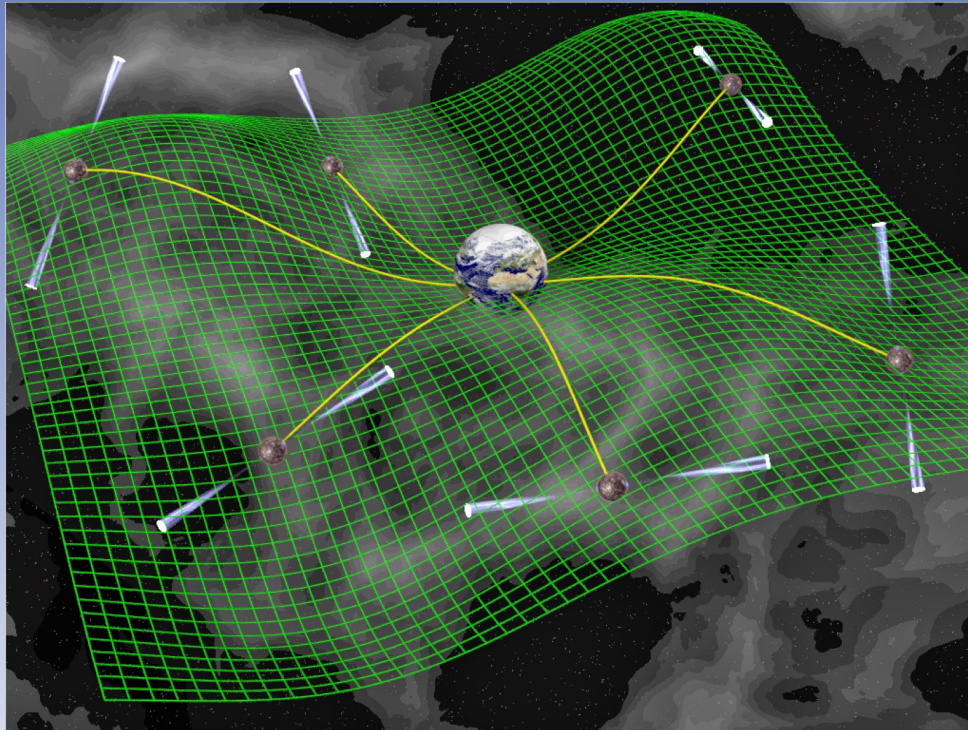


# Impact of planetary ephemerides on Pulsar Timing Arrays results

Aurélien Chalumeau (APC/USN/LPC2E)

G. Theureau (USN/LPC2E), S. Babak (APC), A. Petiteau (APC), L. Guillemot (LPC2E), S. Chen (LPC2E)

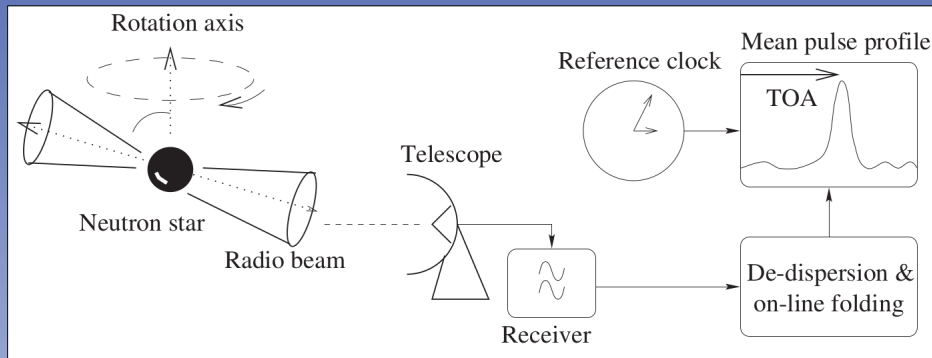


MODE-SNR-PWN Orléans 2019



# The pulsar timing process

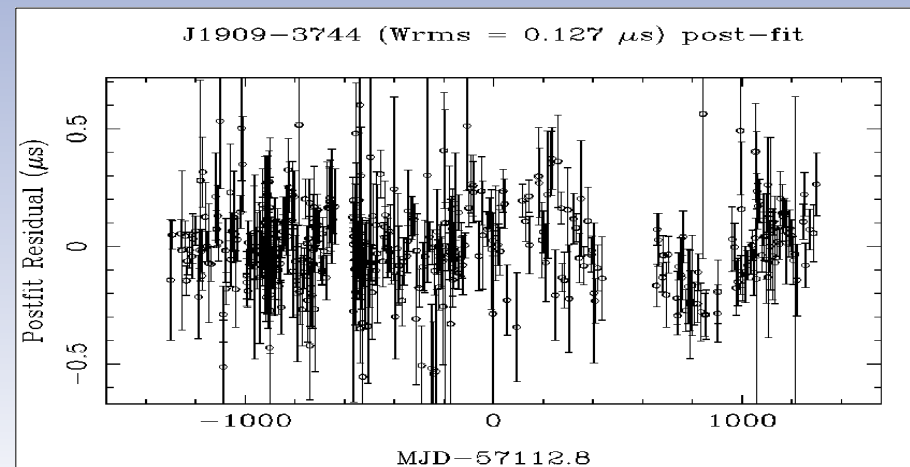
## Observational TOAs



## Timing model

- Rotational params
- Astrometric params
- Orbital params
- ISM effects
- Clock correction
- Transformation to the SSB
- ...

## Residuals

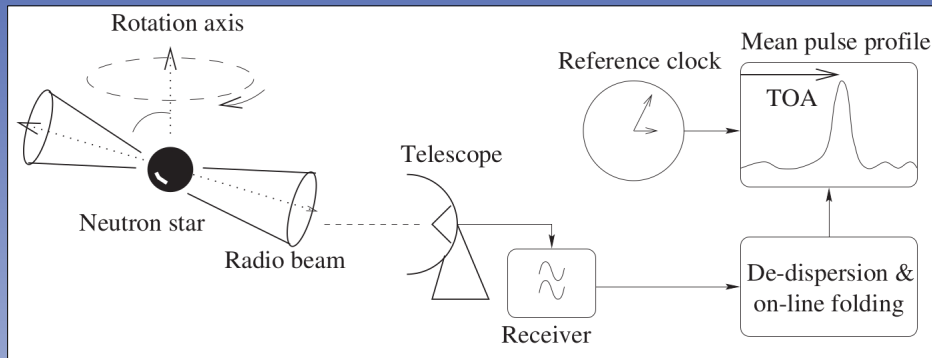


cf. Lorimer & Kramer 2005

MODE-SNR-PWN Orléans 2019

# The pulsar timing process

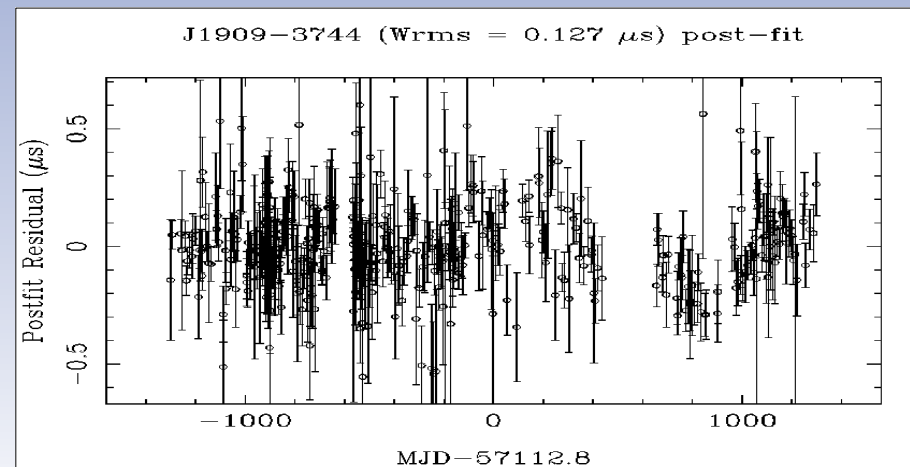
## Observational TOAs



## Timing model

- Rotational params
- Astrometric params
- Orbital params
- ISM effects
- Clock correction
- **Transformation to the SSB**
- ...

## Residuals



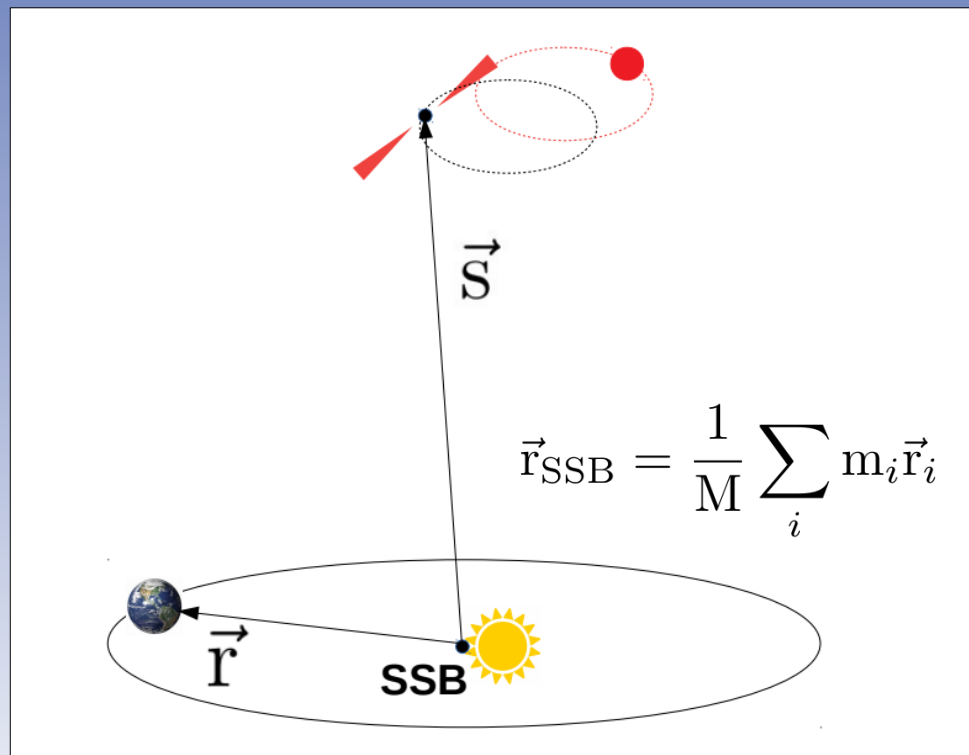
cf. Lorimer & Kramer 2005

MODE-SNR-PWN Orléans 2019

# TOA transformation to the SSB

*From the topocentric to the quasi-inertial solar system barycenter frame*

$$t_{SSB} = t_{topo} + t_{corr} - \Delta D / f_{obs}^2 + \Delta_{R\odot} + \Delta_{\pi} + \Delta_{S\odot} + \Delta_{E\odot}$$



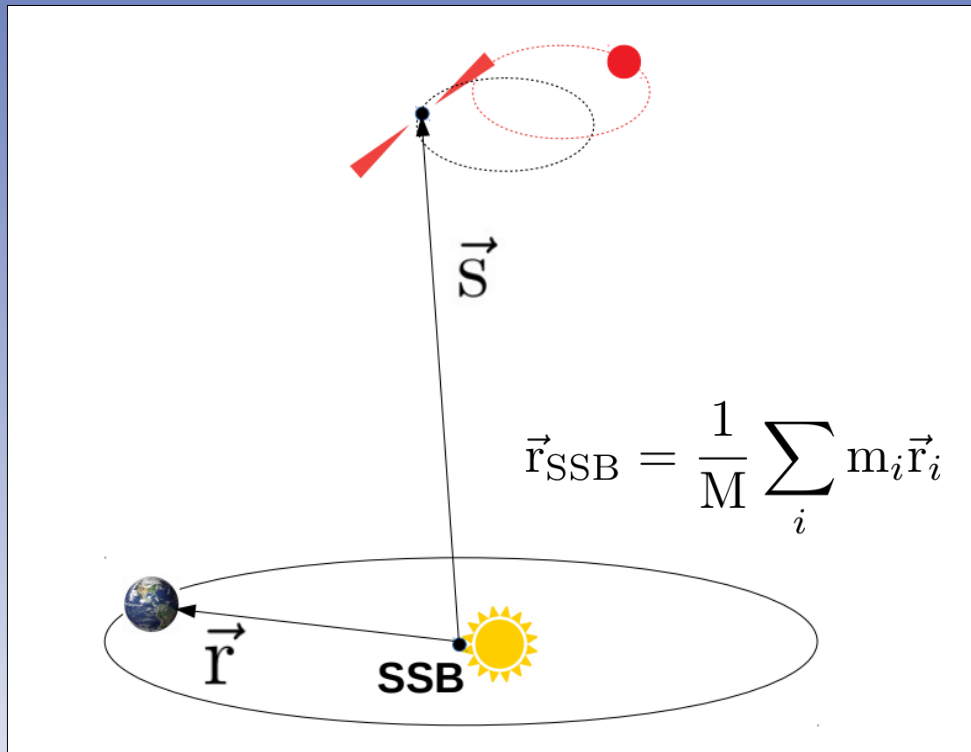
cf. Lorimer & Kramer 2005

MODE-SNR-PWN Orléans 2019

# TOA transformation to the SSB

From the topocentric to the quasi-inertial solar system barycenter frame

$$t_{SSB} = t_{topo} + t_{corr} - \Delta D / f_{obs}^2 + \Delta_{R\odot} + \Delta_{\pi} + \Delta_{S\odot} + \Delta_{E\odot}$$



➔ Orbits of solar system bodies needed !

Römer delay

$$\Delta_{R\odot} = -\frac{1}{c} \vec{r} \cdot \hat{s}$$

Parallax

$$\Delta t_{\pi} = -\frac{1}{2cd} (\vec{r} \times \hat{s})^2$$

Shapiro

$$\Delta_{S\odot} = -2 \sum_i \frac{GM_i}{c^3} \ln \left[ \frac{\hat{s} \cdot \vec{r}_i^E + r_i^E}{\hat{s} \cdot \vec{r}_i^P + r_i^P} \right]$$

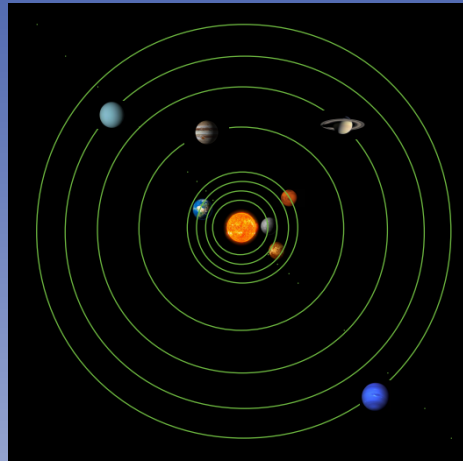
Einstein delay

$$\frac{d\Delta_{E\odot}}{dt} = \sum_i \frac{GM_i}{c^2 r_i^E} + \frac{v_E^2}{2c^2} - \text{constant}$$

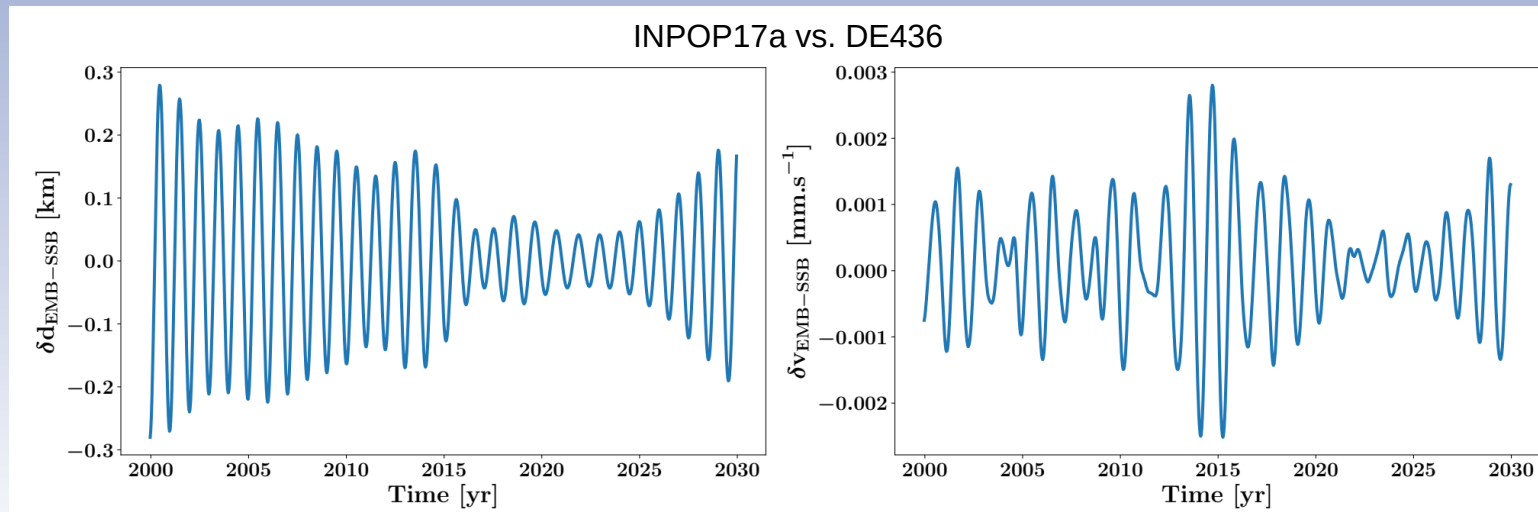
cf. Lorimer & Kramer 2005

# Solar system ephemeris (SSEs)

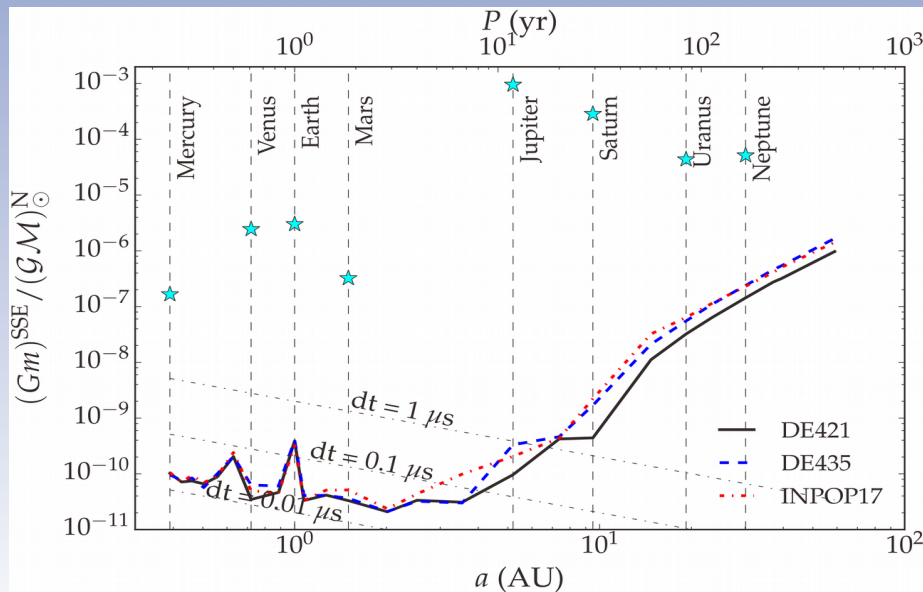
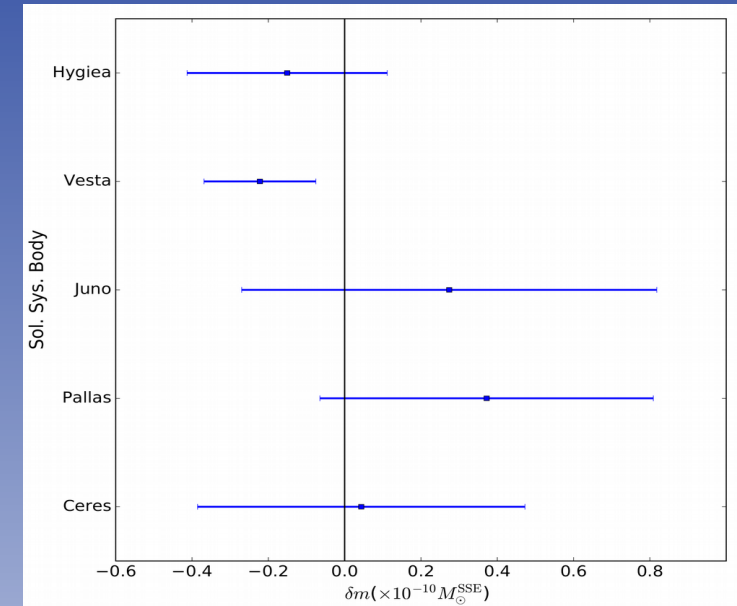
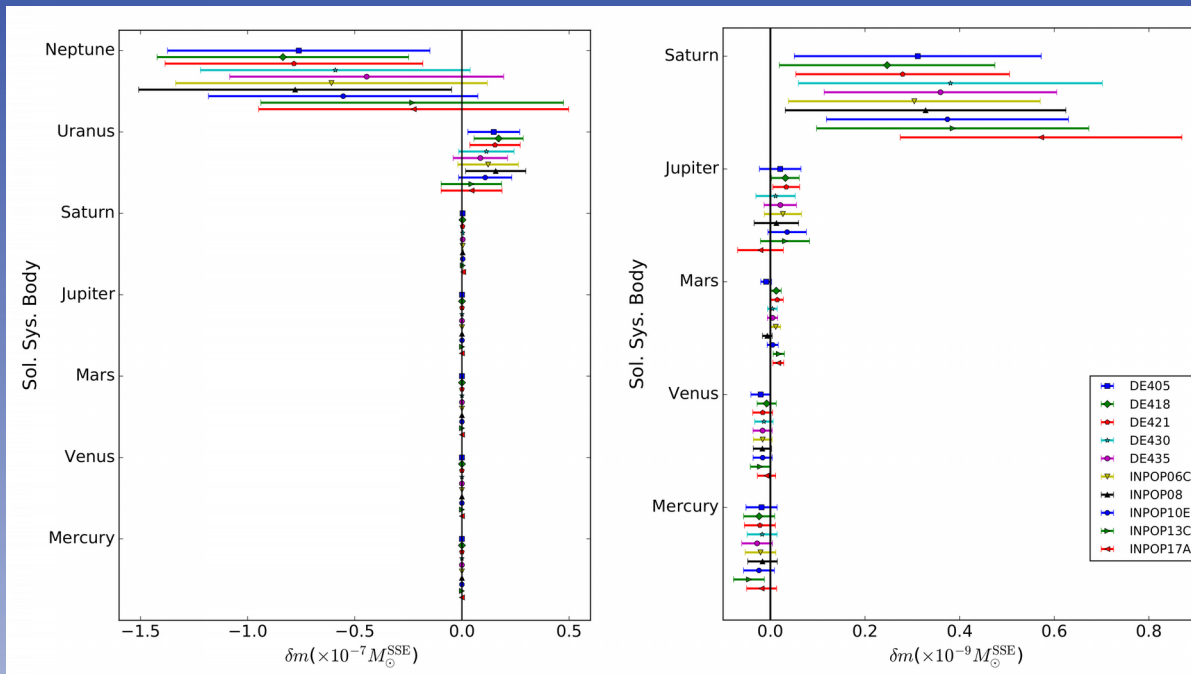
*Predict positions and velocities of solar system bodies*



- ➔ Numerical integration of planetary motion fitted to the observational data
- ➔ SSE produced by JPL, IMCCE, ....



# A possible study : use PTA to constraint SSEs



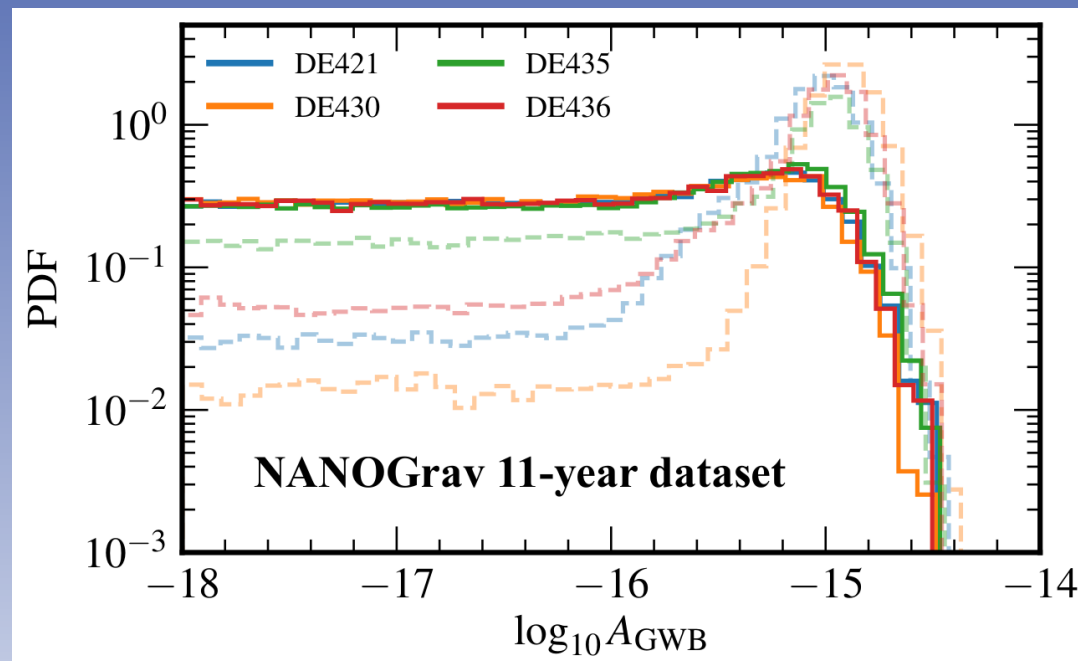
- Mass constraints :
  - Planetary systems
  - Asteroid-belt objects
- Limits on unmodelled object masses
- ULs on putative exotic object mass

cf. Caballero et al. 2018

# Impact of SSEs on PTA results

*Systematic biases larger than the statistical uncertainty of the limits*

***SSE errors can mimic a GWB signal !***



➔ **BAYESEPHM** model (11 parameters) to marginalize  $A_{\text{GWB}}$  over ephemeris uncertainties

➔ **GWB constraint gets robust against SSE errors**

➔ **Problem : Modelling SSE errors can absorb some of the GWB signal**

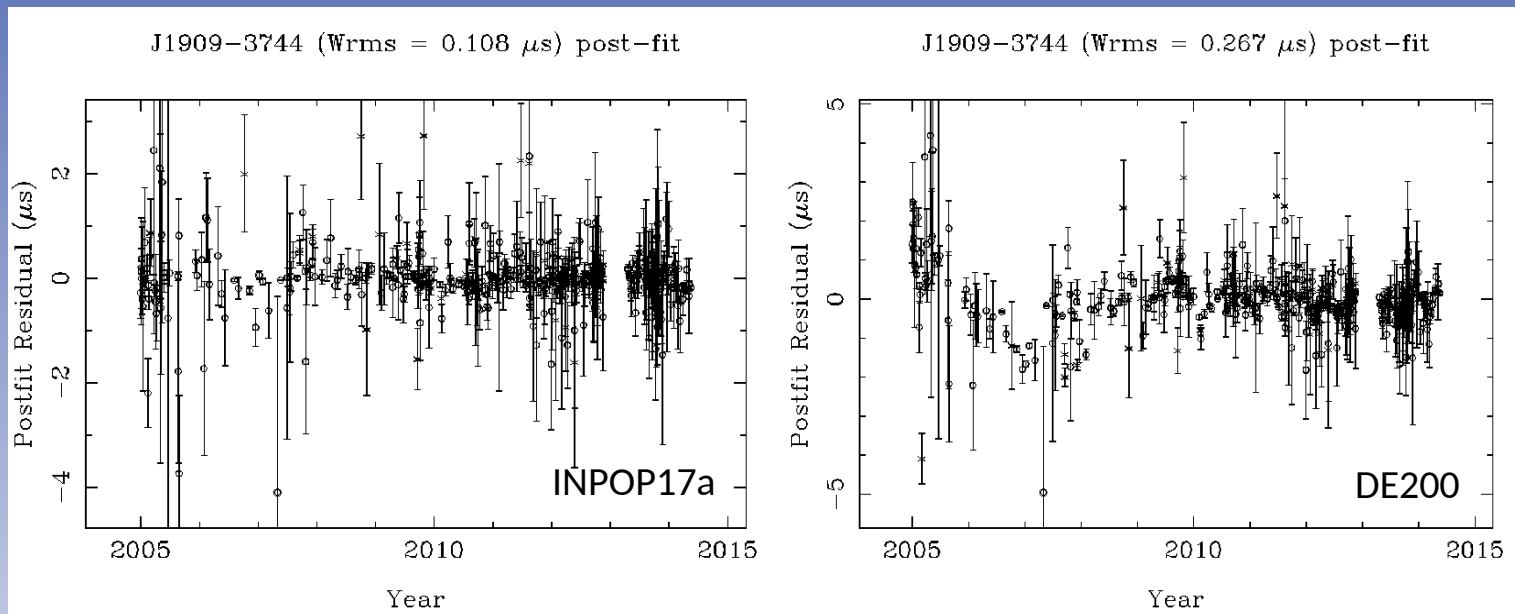
cf. Arzoumanian et al. 2018



# Impact of SSEs on PTA results

## Characterization of the impact of SSE errors

Using **INPOP** data with a direct expert support (cf. **A. Fienga** (Géoazur))

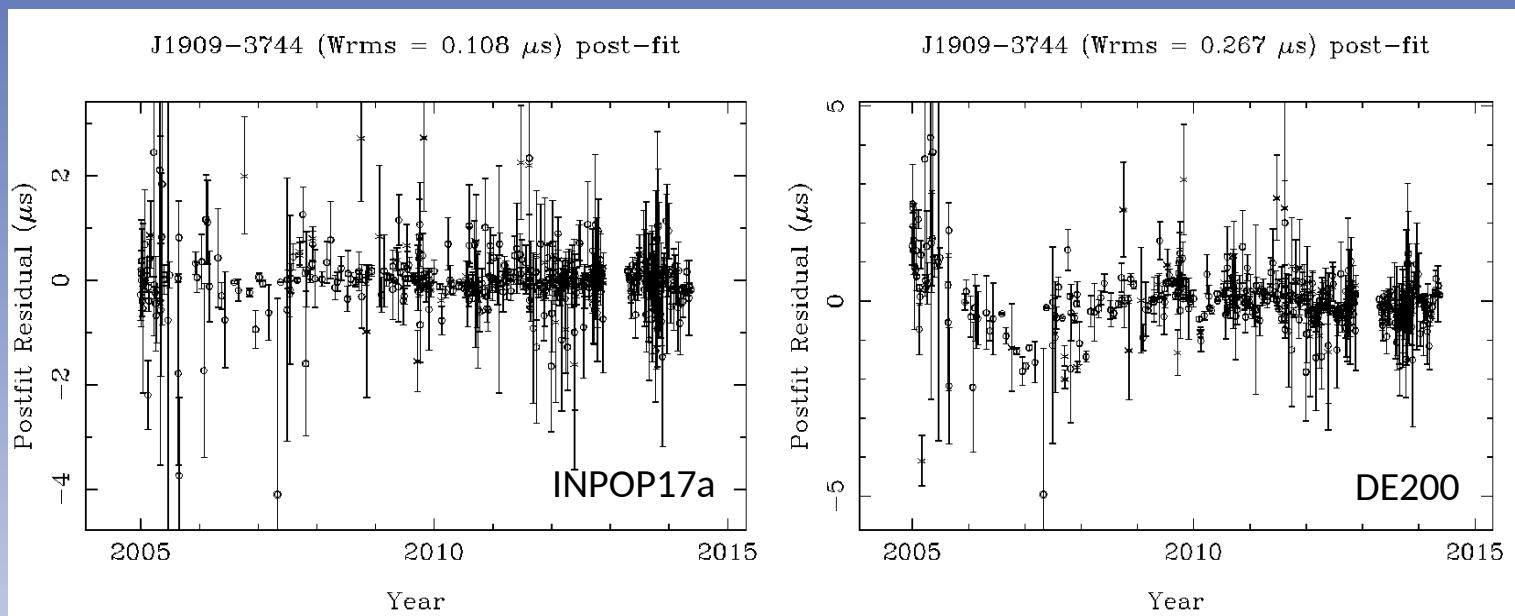



- Production of perturbed SSEs
- Input perturbed SSEs in timing process
- Same for the full GWB search process

# Impact of SSEs on PTA results

## Characterization of the impact of SSE errors

Using **INPOP** data with a direct expert support (cf. **A. Fienga** (Géoazur))



- Production of perturbed SSEs 
- Input perturbed SSEs in timing process
- Same for the full GWB search process

# Impact of SSEs on PTA results

## Production of perturbed SSEs

$$\vec{x}_{new}(\vec{\theta}) = \vec{x}_{ref}(\vec{\theta}) + \frac{\partial \vec{x}_{ref}(\vec{\theta})}{\partial \vec{\theta}} \delta \vec{\theta}$$

Reference (P,V)

$$\vec{x}_{ref}(\vec{\theta})$$

Partial matrices

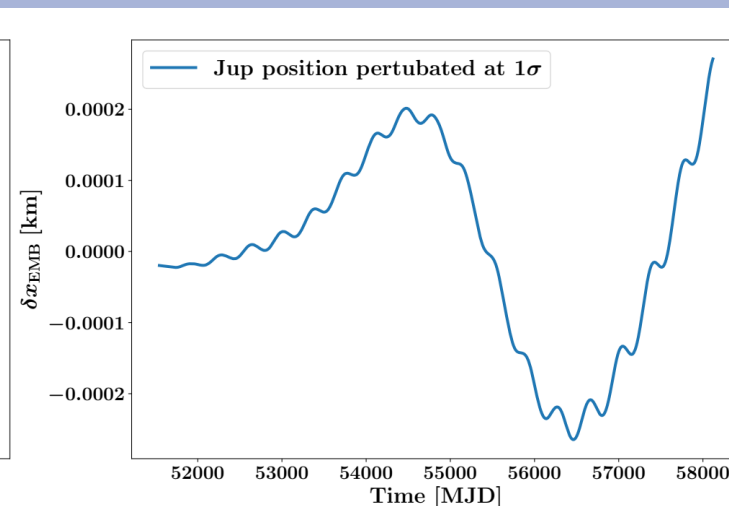
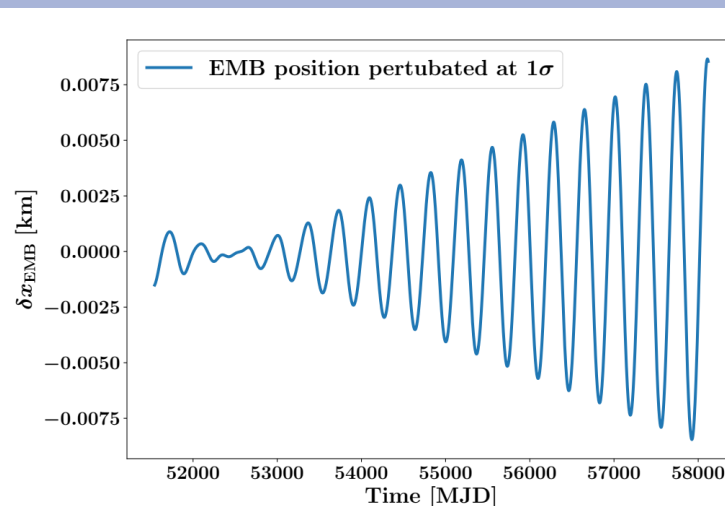
$$\frac{\partial \vec{x}_{ref}(\vec{\theta})}{\partial \vec{\theta}}$$

Covariance matrix

$$\delta \vec{\theta}$$

Orbital elements

$$\vec{\theta} = \begin{pmatrix} a \\ l \\ k(e, \pi) \\ h(e, \pi) \\ q(I, \Omega) \\ p(I, \Omega) \end{pmatrix}$$



# Conclusion

- PTA sensitivity limited by SSE imperfections
- **BAYESEPHÉM** corrects SSE systematics but could subtract the sensitivity
  - Essential to characterize properly the impact on PTA results
- Perturbated SSE produced thanks to A. Fienga – PTA-France group collaboration
- Next steps :
  - Study the effects on timing residuals and pulsar parameters
  - Characterize properly the effects on GW search results